

# Abductive Learning for Neuro-Symbolic Grounded Imitation

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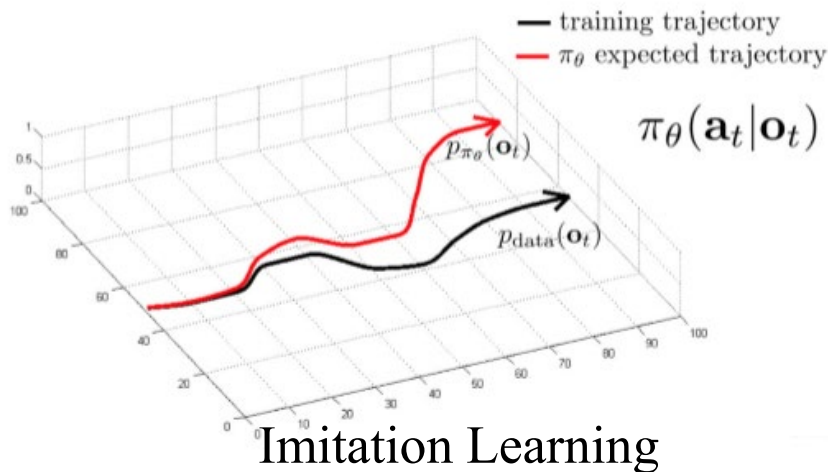
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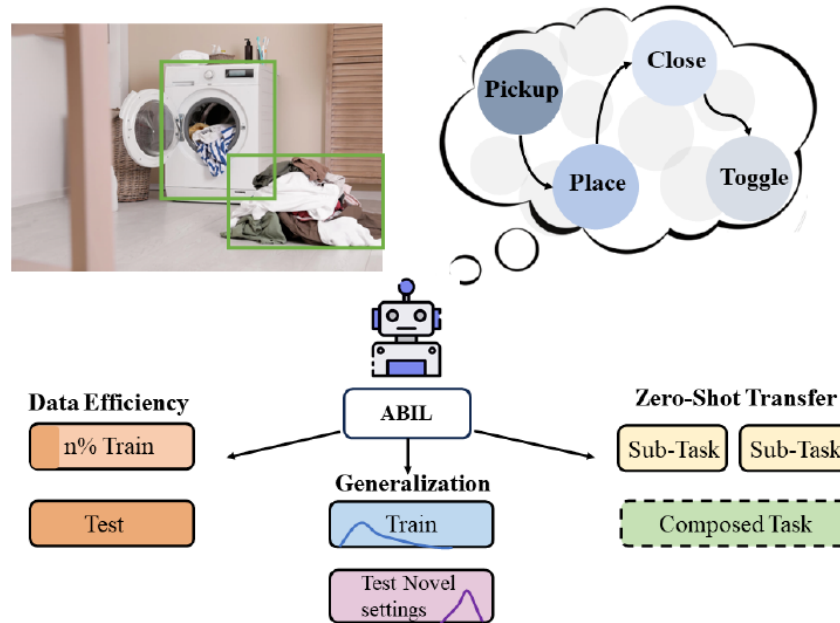
# What is this work about

- Long-Horizon Decision-Making is critical for embodied intelligence.
  - Imitation Learning
    - ✓ Shows promising performance on robotics and auto-driving.
    - Is **limited in open environments**, especially in the **long-horizon tasks**.
  - Traditional symbolic planning
    - ✓ Excels at long-horizon tasks via logical reasoning.
    - Typically abstracts away perception with ground-truth symbols, **struggles to map visual observations to human-defined symbolic spaces**.



Such limitations restrict their application in **Open environments**.

# What is this work about



- ✓ In this work, we propose a novel framework Abductive Imitation Learning (ABIL) to combine the benefits of **data-driven learning** and **symbolic-based reasoning**.
- ✓ Our **ABIL** shows significantly improved performance on settings of **data-efficiency** and **generalization** in the open environments.

## 1. Background

## 2. ABIL Framework

## 3. Empirical Results

## 4. Conclusion

## Background

### ❑ Previous Studies:

- Imitation learning: is weak at long-horizon tasks
- Symbolic Planning: requires symbolic-level grounding
- Recent efforts on neuro-symbolic solutions[1,2,3]:  
These methods typically assume there are **sufficient symbolic information**, or only applicable to **low-dimensional robotics states**.

## Our Goal

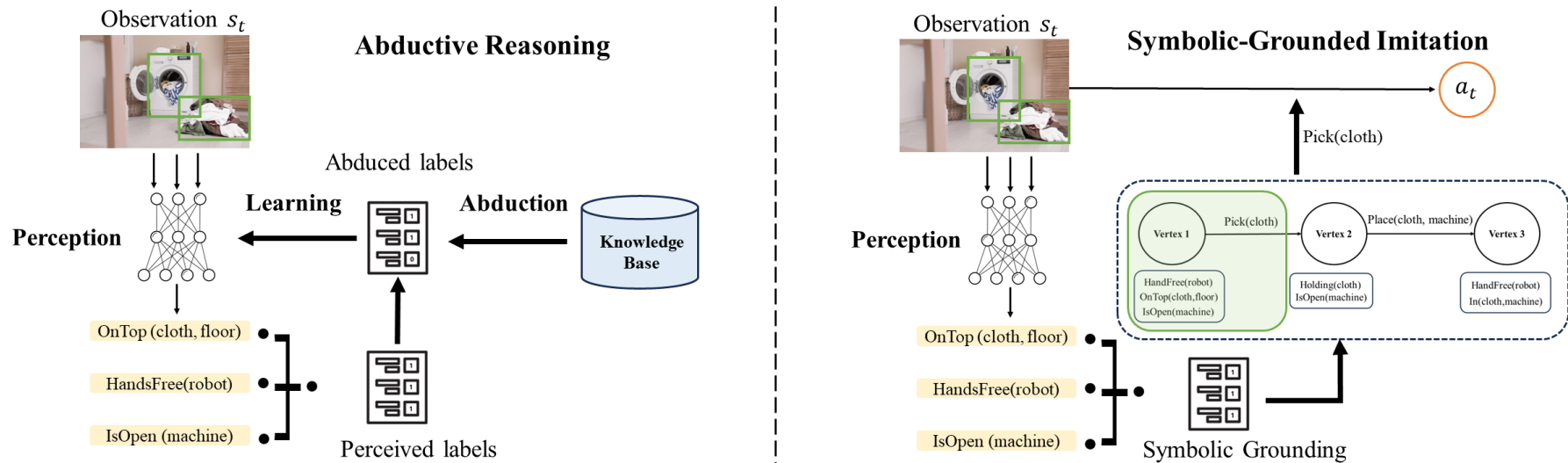
- Help the agent **understand demonstrations in symbolic space** from high-dimensional visual observations **without symbolic-level label**.
- Enable **long-term logical planning** for imitation learning.

[1] Regression Planning Networks. NeurIPS'19

[2] Learning Symbolic Operators for Task and Motion Planning. IROS'21

[3] Programmatically grounded, compositionally generalizable robotic manipulation. ICLR'23

## The Overall Framework



Goal:

- Help the agent **understand demonstrations in symbolic space** from high-dimensional visual observations **without symbolic-level label**.
- Enable **long-term logical planning** for imitation learning.

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Goal-based planning task.

➤ Environment Definition:  $\langle S, \mathcal{A}, \mathcal{T}, O, \mathcal{P}, OP, S^0, g \rangle$

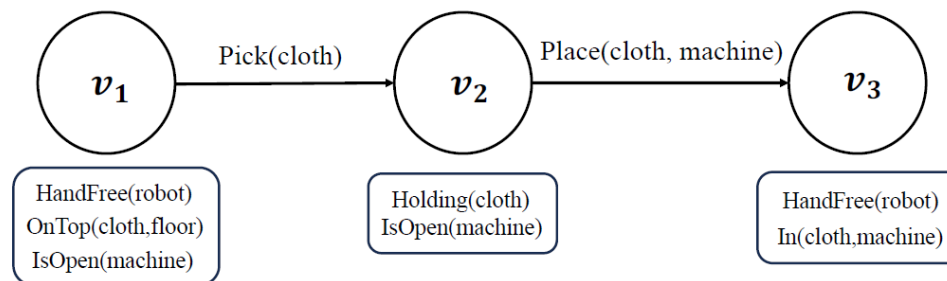
Deterministic, fully-observed environment with object-centric representation.

➤ Symbolic Knowledge Base:

A finite-state machine, with a directed graph  $G = \langle V, E \rangle$

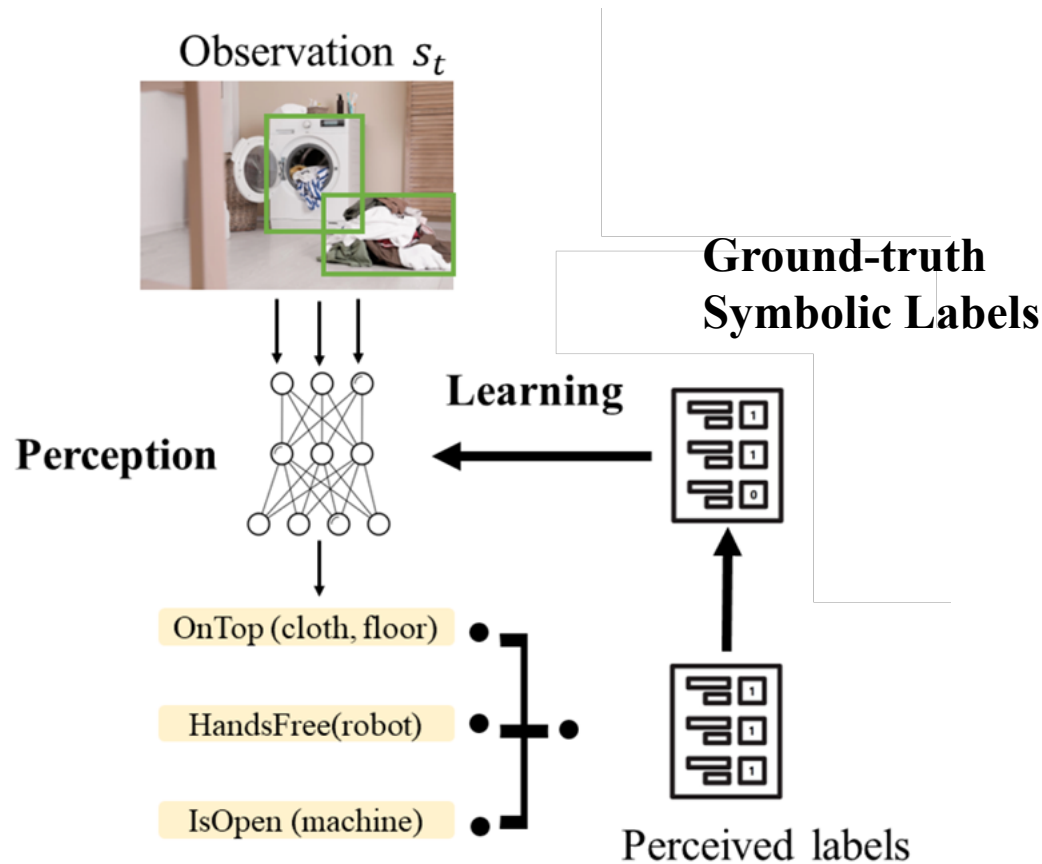
❑ Each node  $v \in V$  contains a set of ground atoms, which can be viewed as the condition of a sub-task.

❑ Each edge is noted as a tuple  $\langle \overline{op}, EFF^+, EFF^- \rangle$ .



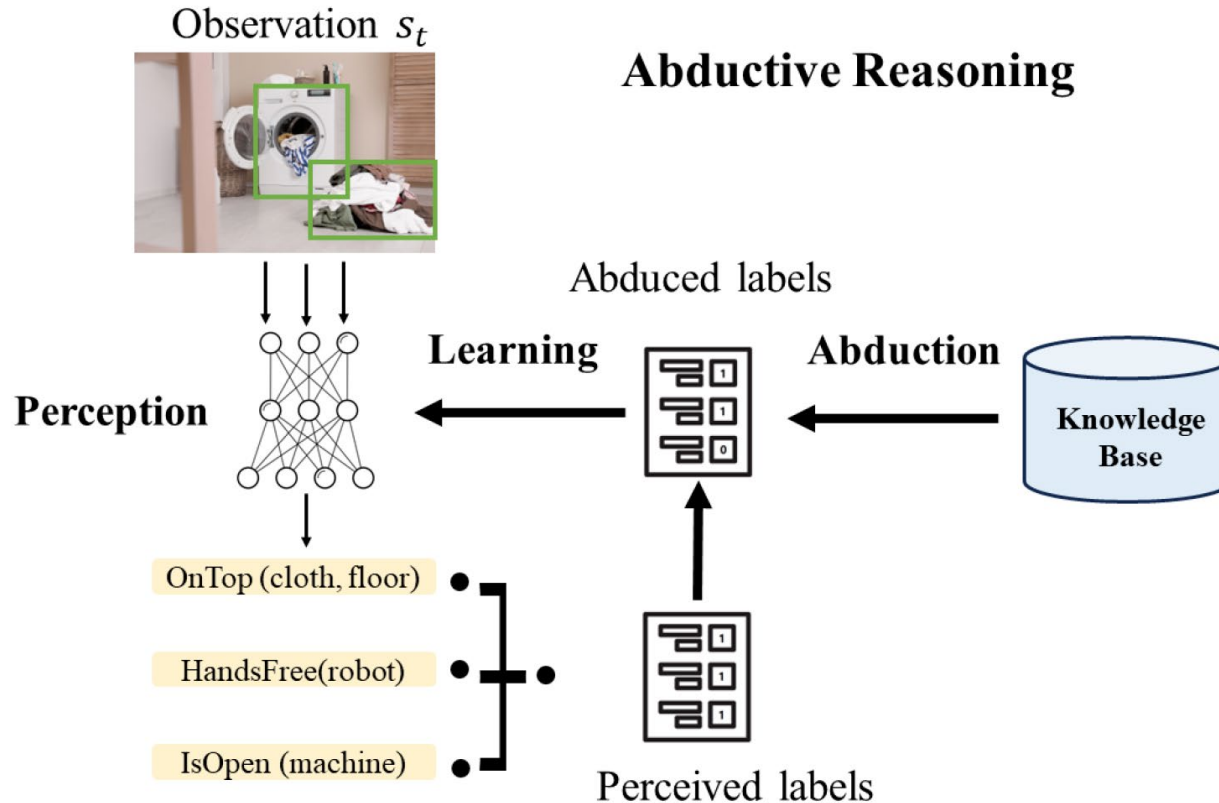
An example of the knowledge base





A straightforward method: optimize the network with the symbolic labels.

However: **Symbolic supervision is typically costly or not available**

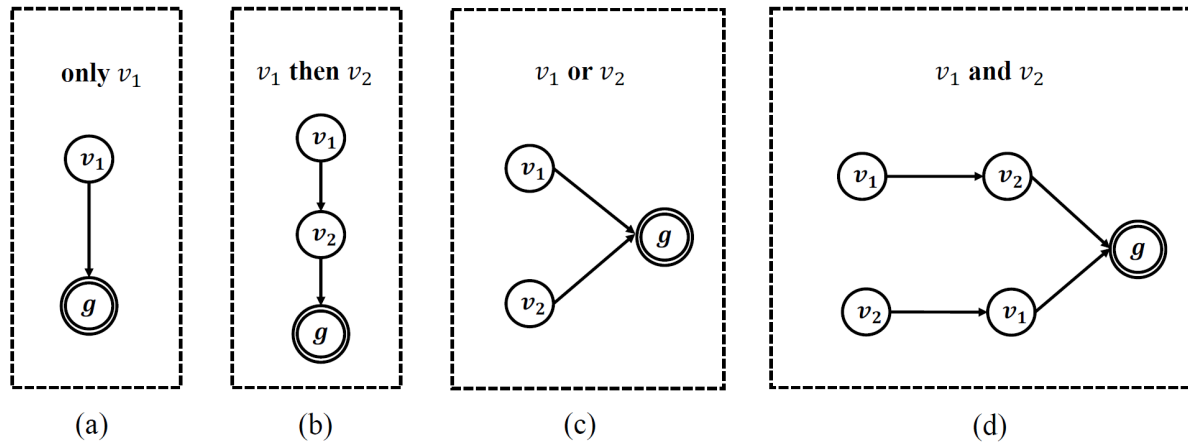


A straightforward method: optimize the network with the symbolic labels.

However: **Symbolic supervision is typically costly or not available**

We introduce the **abductive reasoning** to optimize the network.

- Acquire the **pseudo label** from the **knowledge of state machine** via abductive reasoning.

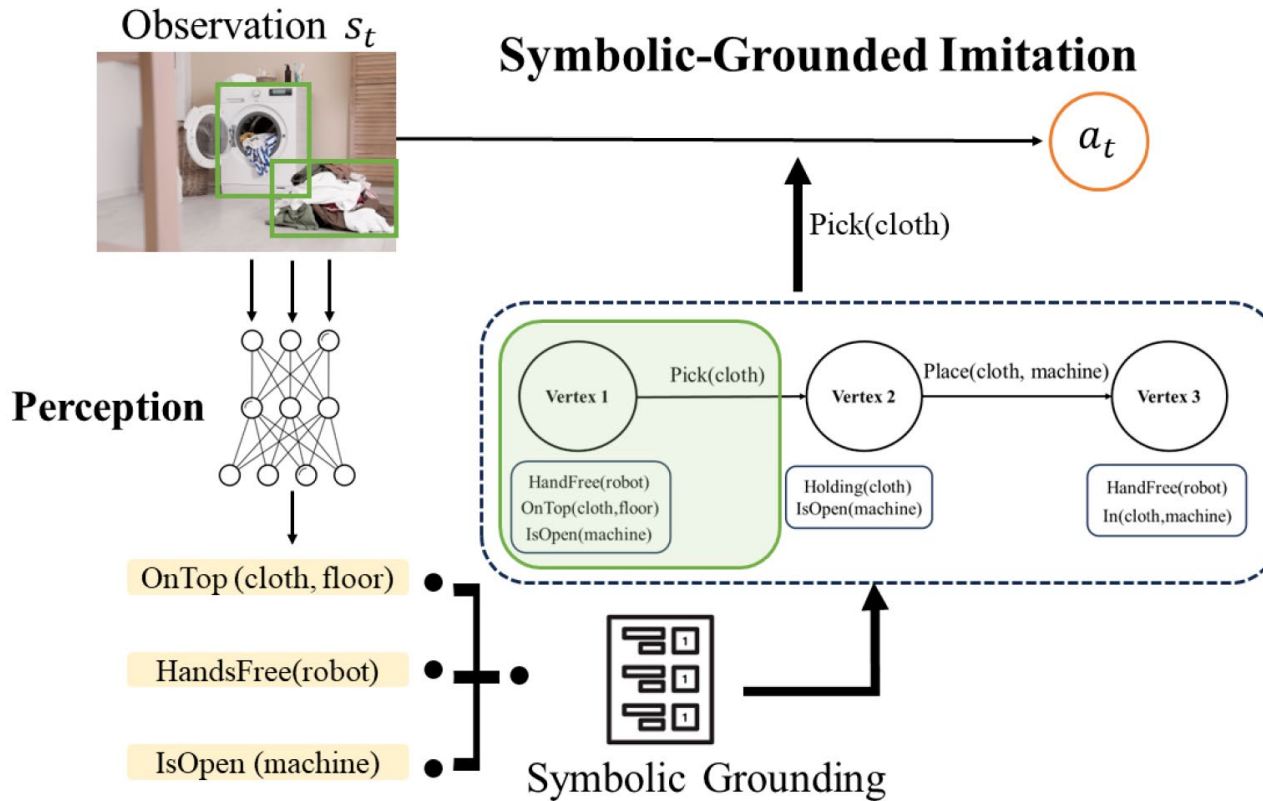


Typical structures of the state machine

- Derive the **sequential abduction**:  $\{z_i^t\}_{t=1}^T \models G$
- Optimize the perception function  $f$

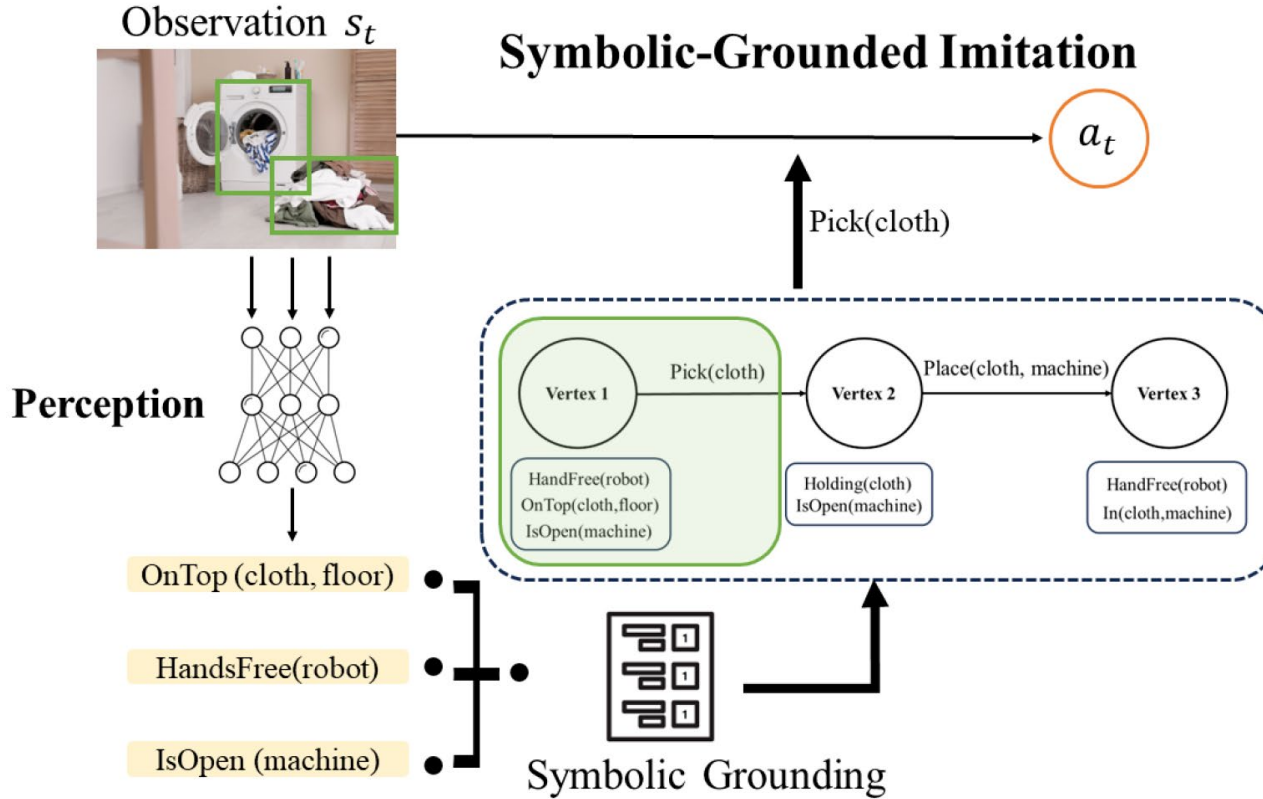
$$\min_f \sum_{s_i \in D} \sum_{t=1}^T \mathcal{L}(f(s_i^t), \hat{z}_i^t),$$

$$\{\hat{z}_i^t\}_{t=1}^T = \arg \min_{\{z_i^t\}_{t=1}^T} \sum \|z_i^t - f(s_i^t)\|^2, \quad \text{s.t. } \{z_i^t\}_{t=1}^T \models G$$



- Build the **behavioral actor** for each logical operator  $h_{op}$ , e.g.  $h_{pick}$ ,  $h_{place}$
- Derive the symbolic states by perception  $f$ , and derive the corresponding abstract logical operator

$$\overline{op}^t = \overline{op}_k, \text{ s.t. } f(s^t) \models v_k, \exists k \in [0, K)$$



- Obtain the desired parameter of the operator  $\overline{op}^t$  by reasoning  $o^t = obj(\overline{op}^t)$
- Then optimize the behavior actors

$$\min_h \sum_{s_i, a_i \in D} \sum_{t=1}^T \mathcal{L}(h_{\overline{op}_i^t}(s_i^t, o^t), a_i^t)$$

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**Algorithm 1** Abductive Imitation Learning

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**Require:** Demonstration dataset  $D$ , symbolic knowledge  $G$ . Number of learning rounds  $N_R$  and  $N_I$ .

```
1: for  $t = 1$  to  $N_R$  do
2:   Get the perceived labels via  $f(s)$ 
3:   Get the abducted labels via Eq. 1.
4:   Update the perception network  $f$ .
5: end for
6: for  $t = 1$  to  $N_I$  do
7:   Get the symbolic states via  $f(s)$ 
8:   Get the logical operator  $\bar{o}p$  via Eq. 2.
9:   Update the behavior network  $h_{\bar{o}p}$  via Eq. 4.
10: end for
11: return Perception  $f$  and behavior  $\{h_{\bar{o}p}\}, \bar{o}p \in \mathcal{OP}$ .
```

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- A two-stage learning algorithm.
- Embed **high-level logical reasoning** into the **imitation learning** process.

1. Background & Problem

2. ABIL Framework

**3. Empirical Results**

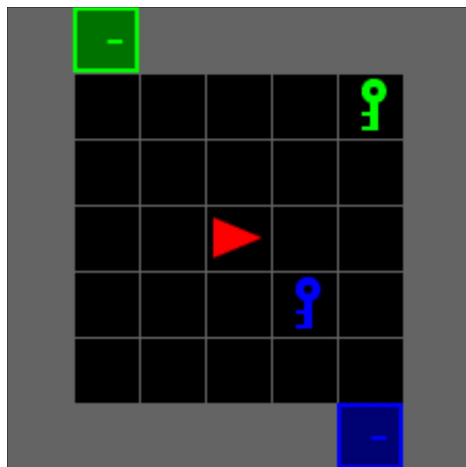
4. Conclusion

## Three diverse environments

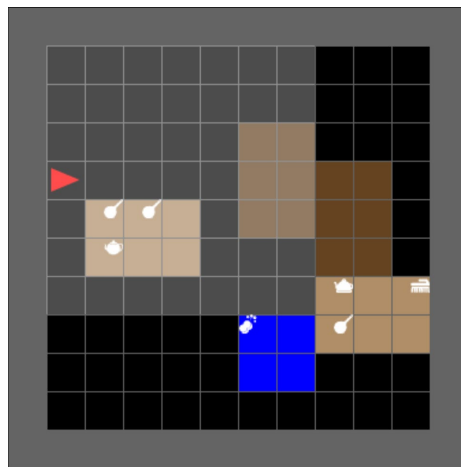
- BabyAI
  - ✓ *Learning with logical instruction*
- Mini-BEHAVIOR
  - ✓ *Household Agent*
- CLIPort
  - ✓ *Robotic manipulation*

## Baseline Methods

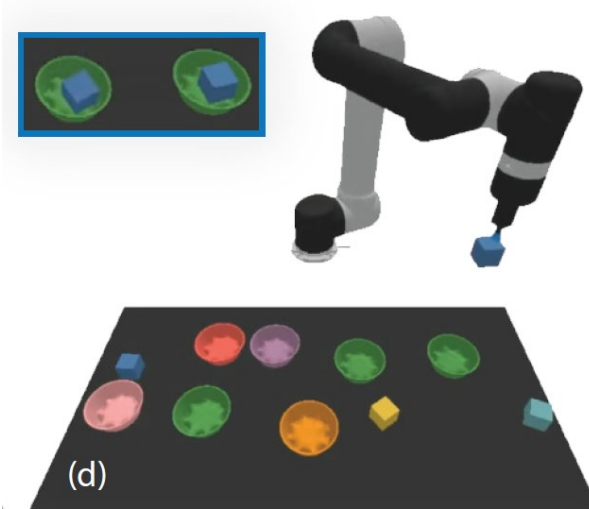
- Behavior Cloning (BC)
- Decision Transformer (DT)
- PDSketch



BabyAI



Mini-BEHAVIOR



CLIPort



Task	Eval	BC	DT	PDSketch	ABIL-BC	ABIL-DT
GotoSingle	Basic	<b>1.00</b>	0.893±0.049	<b>1.00</b>	<b>1.00</b>	<u>0.900±0.036</u>
Goto	Basic	0.843±0.006	0.720±0.044	<b>1.00</b>	<u>0.900±0.046</u>	0.853±0.038
	Gen	0.743±0.045	0.583±0.049	<b>1.00</b>	<u>0.777±0.032</u>	<u>0.793±0.029</u>
Pickup	Basic	0.723±0.031	0.490±0.040	<b>0.990±0.010</b>	<u>0.847±0.025</u>	0.845±0.035
	Gen	0.533±0.031	0.320±0.070	<b>0.973±0.012</b>	<u>0.730±0.010</u>	<u>0.763±0.051</u>
Open	Basic	0.933±0.025	0.493±0.059	<b>1.00</b>	<u>0.963±0.021</u>	0.903±0.064
	Gen	0.877±0.015	0.440±0.078	<b>1.00</b>	<u>0.927±0.032</u>	0.813±0.064
Put	Basic	<b>0.950±0.044</b>	0.910±0.036	0.650±0.026	<u>0.930±0.010</u>	0.920±0.026
	Gen	0.037±0.012	0.207±0.092	0.560±0.052	<b>0.917±0.015</b>	<u>0.877±0.025</u>
Unlock	Basic	0.957±0.012	0.885±0.035	0.293±0.051	<u>0.967±0.023</u>	<b>0.993±0.012</b>
	Gen	0.910±0.030	0.883±0.075	0.247±0.051	<u>0.963±0.006</u>	<b>0.993±0.012</b>
Averaged time per evaluation		0.174 seconds	0.260 seconds	8.17 seconds	0.320 seconds	0.354 seconds

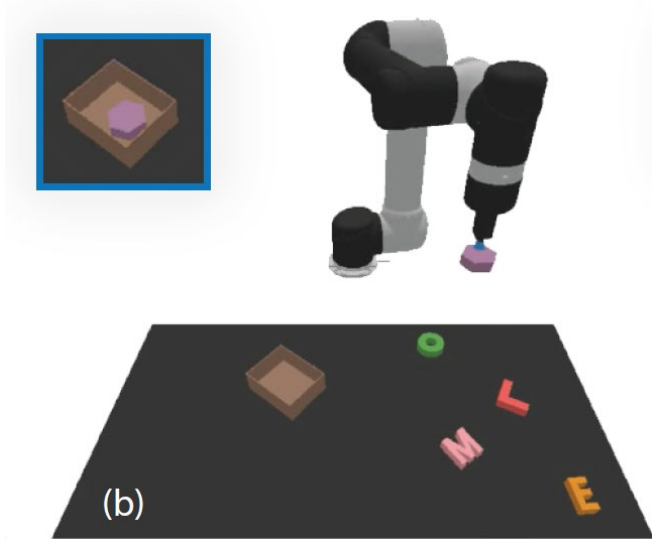
**ABIL** effectively improves the performance of imitation learning methods.

# Results on Mini-BEHAVIOR

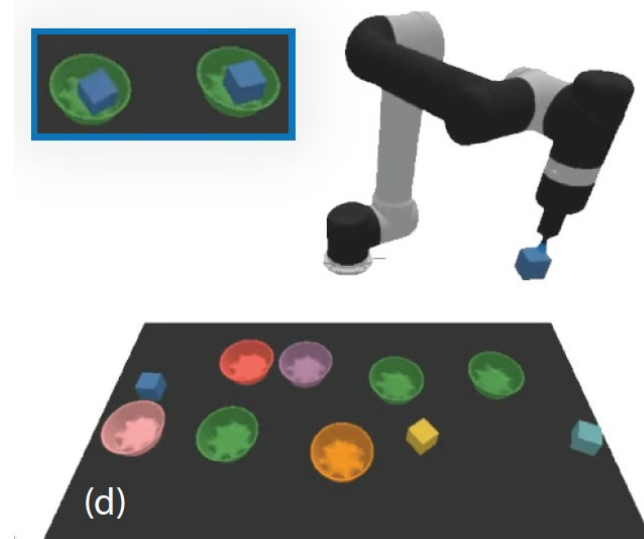
Task	Eval	BC	DT	PDSketch	ABIL-BC	ABIL-DT
Boxing books up	Basic	0.707±0.041	<b>0.713±0.035</b>	> 5 minutes	0.709±0.077	0.661±0.094
	Gen	0.335±0.177	0.519±0.191		<b>0.644±0.172</b>	0.625±0.087
Cleaning A Car	Basic	0.417±0.047	0.313±0.091	> 5 minutes	<b>0.423±0.032</b>	0.330±0.050
	Gen	0.170±0.036	0.147±0.083		<b>0.253±0.047</b>	0.170±0.078
Cleaning shoes	Basic	0.482±0.086	0.427±0.042	> 5 minutes	<b>0.598±0.068</b>	0.478±0.020
	Gen	0.030±0.005	0.053±0.046		<b>0.390±0.102</b>	0.290±0.026
Collect misplaced items	Basic	0.460±0.030	0.299±0.015	> 5 minutes	<b>0.617±0.061</b>	0.457±0.007
	Gen	0.325±0.074	0.261±0.023		<b>0.423±0.051</b>	0.387±0.028
Installing a printer	Basic	0.903±0.023	0.927±0.021	0.343±0.032	0.887±0.021	<b>0.937±0.023</b>
	Gen	0.003±0.006	0.300±0.147	0.310±0.046	0.727±0.047	<b>0.757±0.107</b>
Laying wood floors	Basic	0.616±0.062	0.638±0.027	> 5 minutes	<b>0.644±0.043</b>	0.643±0.031
	Gen	0.068±0.018	0.366±0.041		<b>0.628±0.057</b>	0.374±0.040
Making tea	Basic	0.607±0.015	0.583±0.105	> 5 minutes	<b>0.687±0.038</b>	0.607±0.029
	Gen	0.070±0.078	0.113±0.105		0.370±0.131	<b>0.493±0.124</b>
Moving boxes to storage	Basic	0.753±0.083	0.780±0.017	> 5 minutes	0.767±0.012	<b>0.787±0.032</b>
	Gen	0.417±0.110	0.617±0.042		<b>0.730±0.017</b>	0.673±0.119
Opening packages	Basic	0.947±0.045	0.963±0.034	0.020±0.010	0.978±0.010	<b>0.990±0.009</b>
	Gen	0.295±0.180	0.548±0.065	0.020±0.010	0.905±0.018	<b>0.918±0.033</b>
Organizing file cabinet	Basic	0.156±0.047	0.522±0.067	> 5 minutes	0.231±0.021	<b>0.562±0.037</b>
	Gen	0.083±0.012	0.382±0.112		0.095±0.009	<b>0.454±0.074</b>
Putting away dishes	Basic	0.811±0.031	0.828±0.052	> 5 minutes	<b>0.883±0.043</b>	0.813±0.022
	Gen	0.141±0.111	0.547±0.296		<b>0.830±0.013</b>	0.739±0.072
Sorting books	Basic	0.601±0.032	0.543±0.053	> 5 minutes	0.618±0.012	<b>0.631±0.055</b>
	Gen	0.131±0.047	0.220±0.010		0.338±0.078	<b>0.412±0.038</b>
Throwing away leftovers	Basic	0.833±0.080	0.890±0.029	> 5 minutes	<b>0.924±0.014</b>	0.888±0.039
	Gen	0.222±0.167	0.653±0.039		0.713±0.069	<b>0.729±0.031</b>
Washing pots and pans	Basic	0.342±0.022	0.227±0.079	> 5 minutes	<b>0.349±0.063</b>	0.184±0.024
	Gen	0.099±0.168	0.028±0.016		<b>0.242±0.110</b>	0.153±0.024
Watering houseplants	Basic	0.814±0.034	0.806±0.020	> 5 minutes	<b>0.843±0.010</b>	0.835±0.022
	Gen	0.002±0.004	0.187±0.113		0.545±0.151	<b>0.734±0.063</b>
Averaged time per evaluation		1.48 seconds	2.09 seconds	> 5 minutes	2.88 seconds	2.98 seconds

**ABIL** demonstrates great performance under the open environments.

Task	BC	DT	ABIL-BC	ABIL-DT
Packing-5shapes	0.580±0.252	0.607±0.223	<b>0.983±0.015</b>	0.903±0.085
Packing-20shapes	0.207±0.006	0.180±0.026	<b>0.940±0.030</b>	0.857±0.025
Put-4blocks-in-5bowl	0.365±0.141	0.319±0.068	<b>0.962±0.012</b>	0.917±0.033



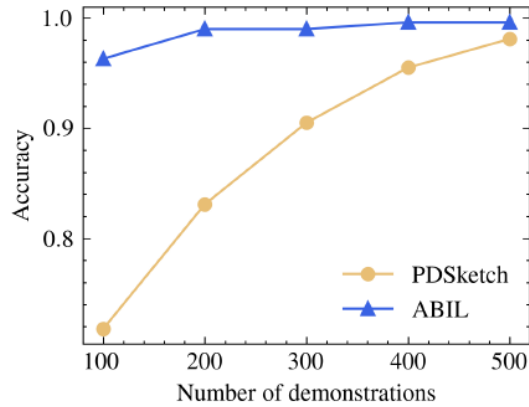
Packing-shapes



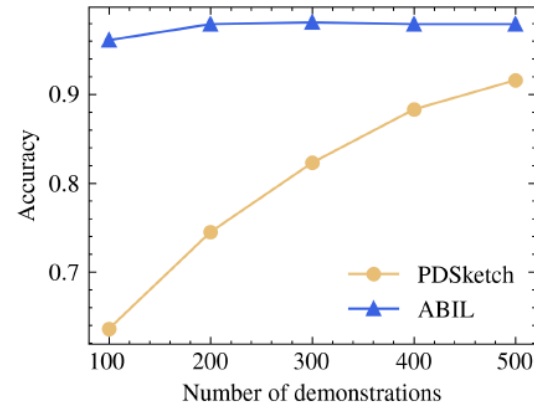
Put-blocks-in-bowls

**ABIL** gives outstanding results in CLIPort Environment.

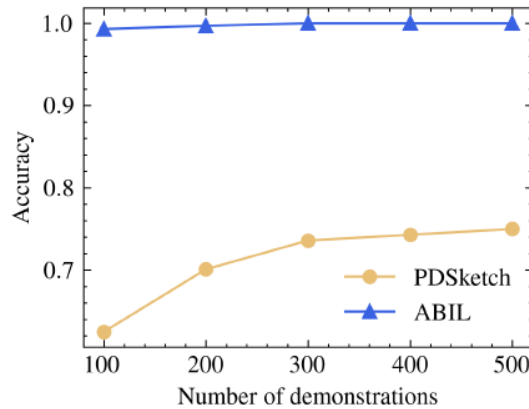
# Comparison of Neural-Symbolic Grounding



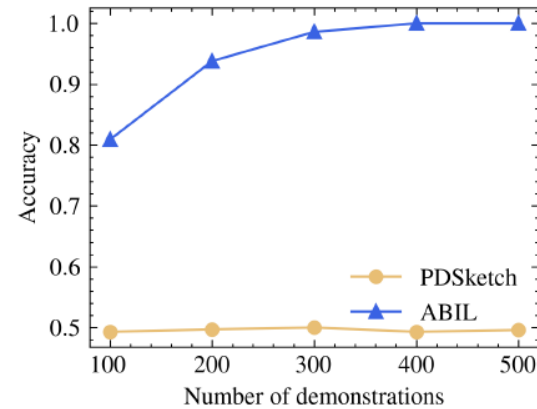
(a) Goto



(b) Pickup

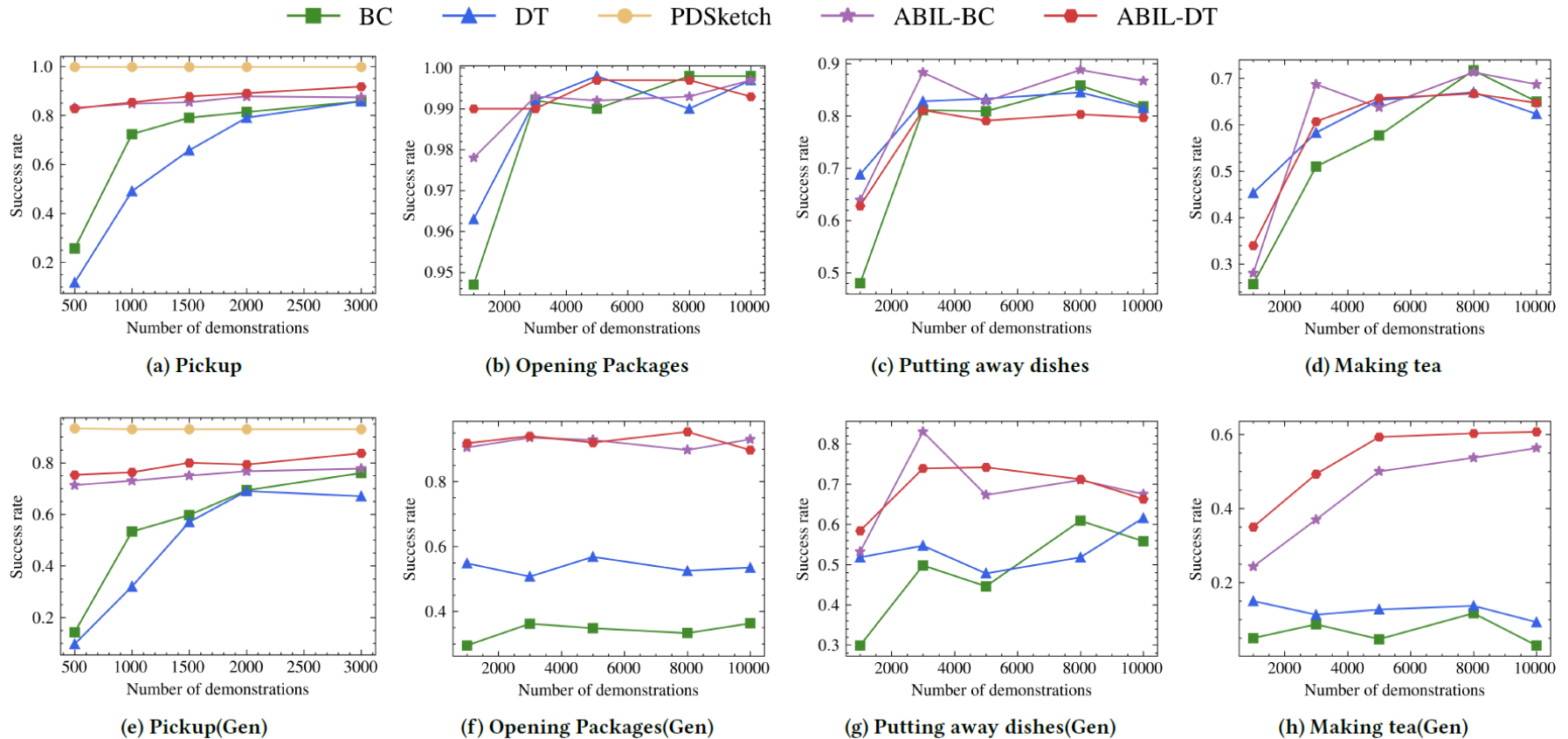


(c) Open



(d) Unlock

**ABIL** outperforms in **understanding the environment** accurately.



**ABIL** improves the **data efficiency** of the BC and DT baselines, achieves significant **generalization improvement** in the out-of-distribution evaluation

Domain	BabyAI		
Task	Train		Eval
	Pickup	Open	Unlock
BC	0.760±0.056	0.983±0.021	0.120±0.010
DT	0.783±0.031	0.957±0.031	0.057±0.051
PDSketch	<b>0.970±0.010</b>	0.990±0.010	0.127±0.021
ABIL-BC	0.937±0.021	<b>1.00</b>	0.980±0.026
ABIL-DT	0.925±0.007	<b>1.00</b>	<b>0.993±0.012</b>

Domain	Mini-BEHAVIOR					
Task	Train	Eval		Train	Eval	
	Open 1	Open 2	Open 3	Throw 1	Throw 2	Throw 3
BC	0.950±0.087	0.012±0.010	0.002±0.004	0.703±0.085	0.117±0.070	0.053±0.045
DT	<b>1.00</b>	0.037±0.025	0.024±0.008	0.770±0.026	0.182±0.008	0.056±0.003
PDSketch	0.467±0.057	0.020±0.010	> 5 minutes	0.013±0.006	> 5 minutes	> 5 minutes
ABIL-BC	0.997±0.006	0.818±0.014	0.551±0.032	0.763±0.049	0.638±0.052	0.536±0.082
ABIL-DT	<b>1.00</b>	<b>0.840±0.035</b>	<b>0.631±0.041</b>	<b>0.803±0.051</b>	<b>0.650±0.049</b>	<b>0.585±0.120</b>

**ABIL** has the ability to **zero-shot generalize** to novel composed tasks.

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- In this paper, we propose a novel framework: ABIL
- ✓ A novel framework which combines the benefits of data-driven learning and symbolic-based reasoning.
- ✓ Extensive experiments demonstrate the effectiveness and generality of ABIL.

## Future work

- Learning with accurate and incomplete knowledge base

# Thank you!

If you are interested in, feel free to contact us:

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